

MA161 SEMESTER 1, CALCULUS: PROBLEM SHEET 4

1. Find
 - (a) $\log_{10} 1\,000\,000$
 - (b) $\log_2 1024$
 - (c) $\log_3 6561$
2. Find, correct to 3 decimal places
 - (a) $\log_2 15$
 - (b) $\log_2 56.25$
 - (c) $\log_3 16$
3. If a certain bacteria population starts with 100 bacteria and doubles every five hours, then the number of bacteria after t hours is given by the function

$$P(t) = 100 \times 2^{t/5}.$$

When will the population reach 25600?

4. The isotope Bismuth-210 has a half-life of 5 days, which means that, compared to time t (in days), only half of the substance remains at time $t + 5$.
 - (a) If there are 50g present at time $t = 0$, show that the quantity remaining at time t can be described by the function

$$f(t) = 50 \times \left(\frac{1}{2}\right)^{t/5}$$

- (b) How many days must pass for the mass to reduce from 50g to less than 1g?